

Detecting and Reducing Model Dependence in Causal Inference

Gary King

March 8, 2006

- Gary King and Langche Zeng. “When Can History be Our Guide? The Pitfalls of Counterfactual Inference,” *International Studies Quarterly*, 2006, forthcoming.

References

- Gary King and Langche Zeng. “When Can History be Our Guide? The Pitfalls of Counterfactual Inference,” *International Studies Quarterly*, 2006, forthcoming.
- Gary King and Langche Zeng. “The Dangers of Extreme Counterfactuals,” *Political Analysis*, Vol. 14, No. 2, 2006, forthcoming.

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<http://GKing.Harvard.edu>

Model Dependence in Practice

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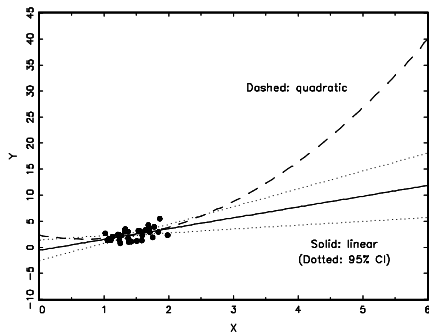
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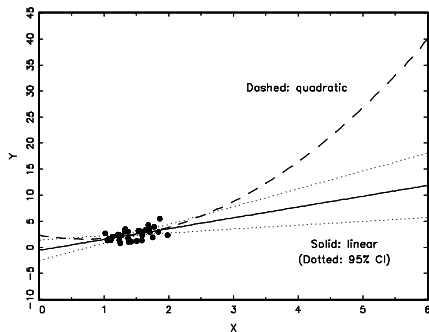
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 - Is this a true test of an *ex ante* hypothesis or merely a demonstration that it is *possible* to find results consistent with your favorite hypothesis?

Which model would you choose? (Both fit the data well.)

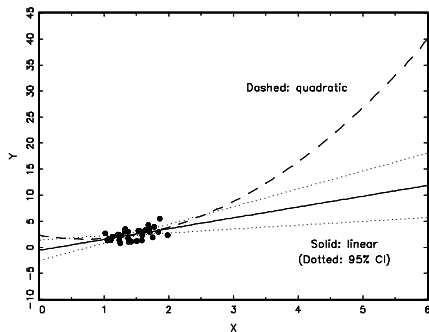


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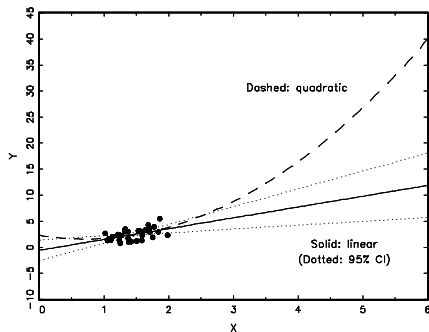
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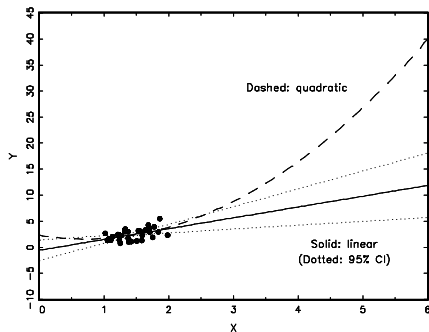
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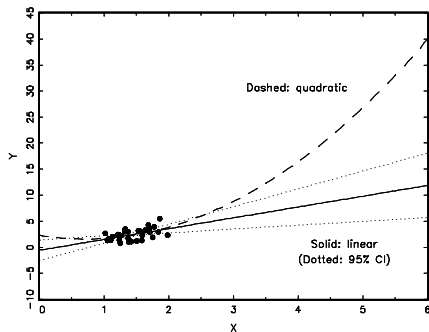
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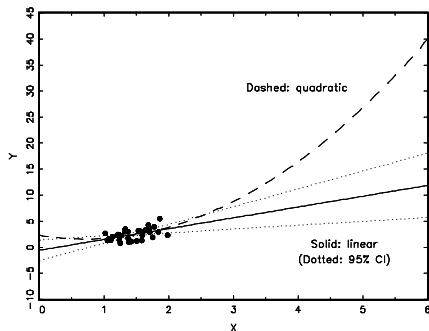
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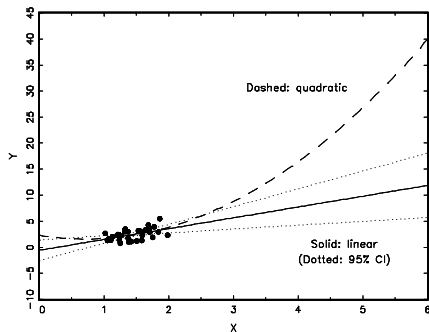
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- How do you choose a model? R^2 ? Some “test”? “Theory”?
- The bottom line: answers to some questions don't exist in the data.
- Same for what-if questions, predictions, and causal inferences

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- If X were continuous, we would be reducing ∞ to 2, also by assumption.

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- If we run a regression, we are summarizing 100 parameters with 3 (an intercept and two slopes).
- But what about including an interaction? Right, so now we're summarizing 100 parameters with 4.
- The difference is still one enormous assumption based on convenience, and neither evidence nor theory.

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- The curse of dimensionality introduces huge assumptions, often recognized.

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 - Results of one run apply to the class of all models, all estimators, and all dependent variables.

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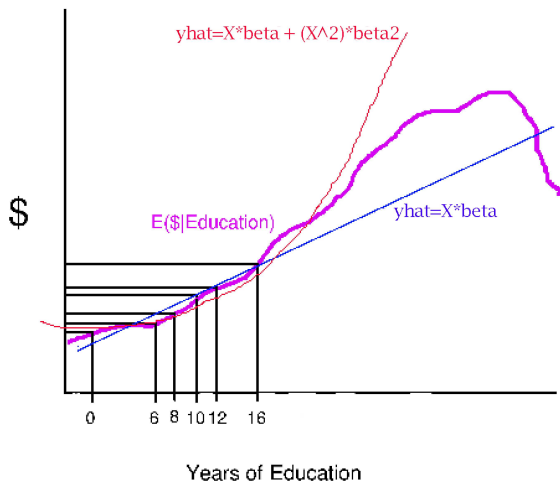
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The maximum degree of model dependence: solely a function of the **distance from the counterfactual to the data**

Interpolation vs Extrapolation in one Dimension



Interpolation or Extrapolation in One and Two Dimensions

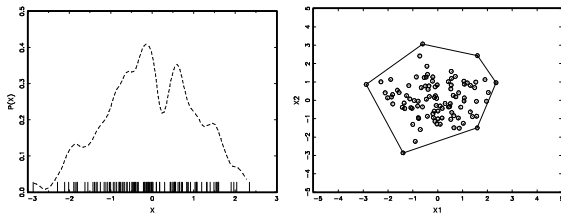


Figure: The Convex Hull

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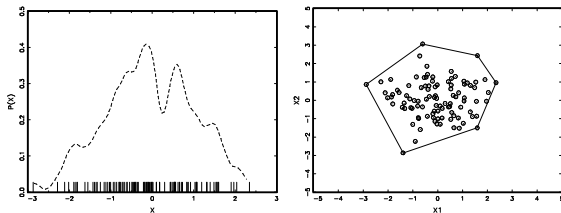


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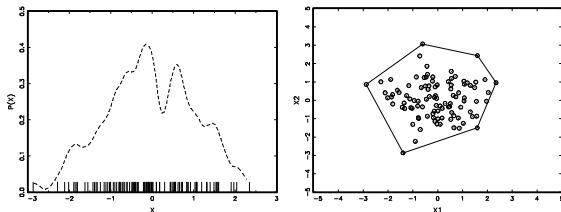


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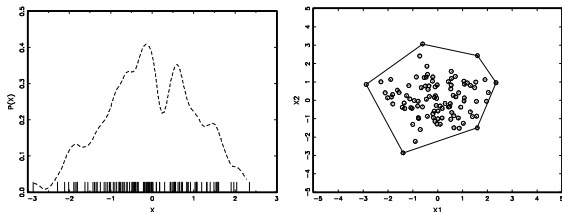


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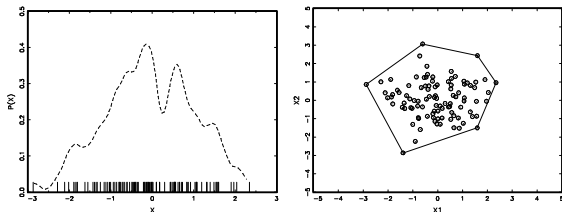


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- We show how to determine whether a point is in the hull without calculating the hull, so its fast; see <http://GKing.harvard.edu/whatif>

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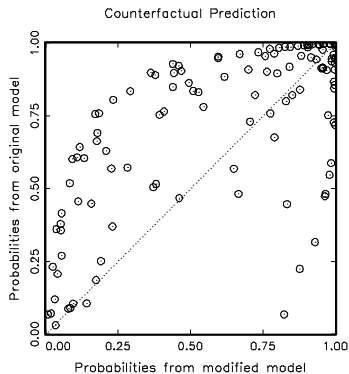
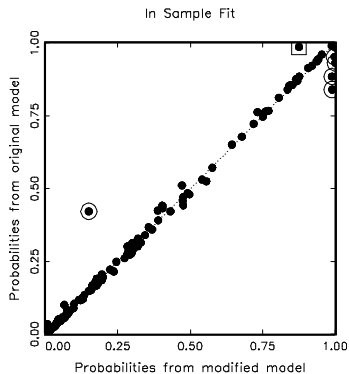
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- Thus, without estimating any models, we know inferences will be model dependent; for illustration, let's find an example. . . .

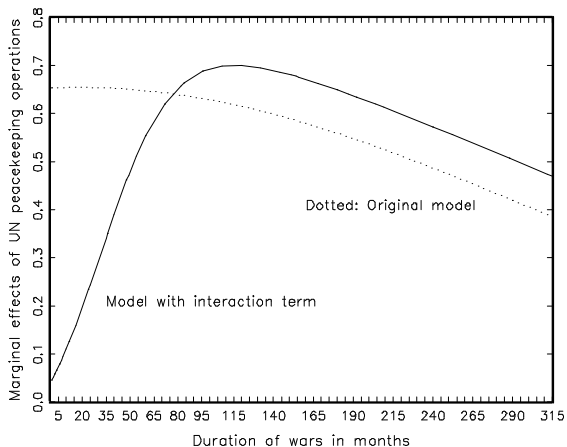
Doyle and Sambanis, Logit Model

Variables	Original Model			Modified Model		
	Coeff	SE	P-val	Coeff	SE	P-val
Wartype	-1.742	.609	.004	-1.666	.606	.006
Logdead	-.445	.126	.000	-.437	.125	.000
Wardur	.006	.006	.258	.006	.006	.342
Factnum	-1.259	.703	.073	-1.045	.899	.245
Factnum2	.062	.065	.346	.032	.104	.756
Trnsfcap	.004	.002	.010	.004	.002	.017
Develop	.001	.000	.065	.001	.000	.068
Exp	-6.016	3.071	.050	-6.215	3.065	.043
Decade	-.299	.169	.077	-0.284	.169	.093
Treaty	2.124	.821	.010	2.126	.802	.008
UNOP4	3.135	1.091	.004	.262	1.392	.851
Wardur*UNOP4	—	—	—	.037	.011	.001
Constant	8.609	2.157	0.000	7.978	2.350	.000
N		122			122	
Log-likelihood		-45.649			-44.902	
Pseudo R^2		.423			.433	

Doyle and Sambanis: Model Dependence



Causal Effect of Multidimensional UN Peacekeeping



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 - resulting estimates are less model dependent.

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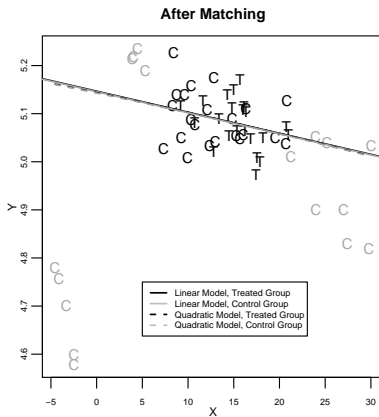
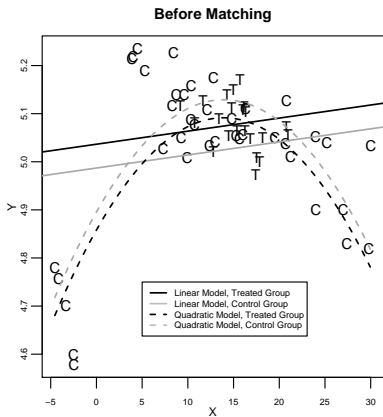
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 - $p(X | t_i = 1) = p(X | t_i = 0)$ or $p(X | t_i = 1) \approx p(X | t_i = 0)$.

A Matching Example



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- Exact matching: for every value of $X = x$ and $t = 0$, we have another for which $X = x$ and $t = 1$. Then by definition, $p(X|t = 1) = p(X|t = 0)$ holds
- Normally, we will only approximate this goal, and will sacrifice some bias reduction (due to lack of balance) for more observations.

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- All easy to do with **MatchIt** and **Zelig**

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- 18 control variables (clinical factors, firm characteristics, media variables, etc.)

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- (Normal applications would only do one or a small number of specifications.)

Example of Balance Tests

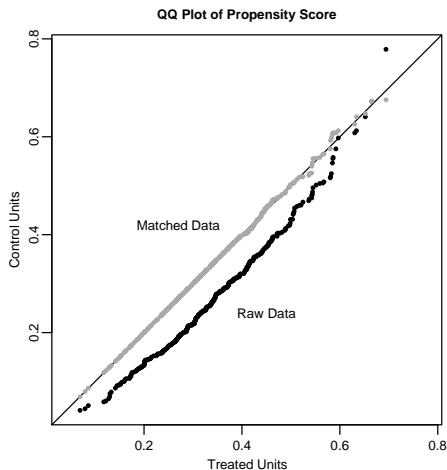


Figure: QQ plot of propensity score

Reducing Model Dependence

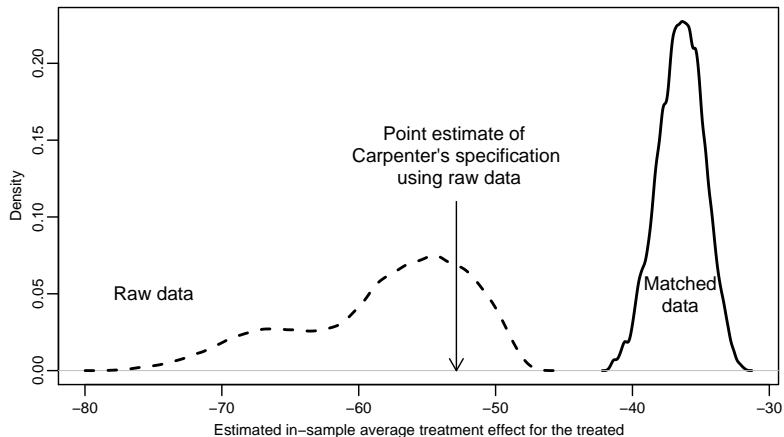


Figure: Histogram of estimated in-sample average treatment effect for the treated (ATT) of the Democratic Senate majority on FDA drug approval time across 262,143 specifications.

Another Example: Jeffrey Koch, AJPS, 2002

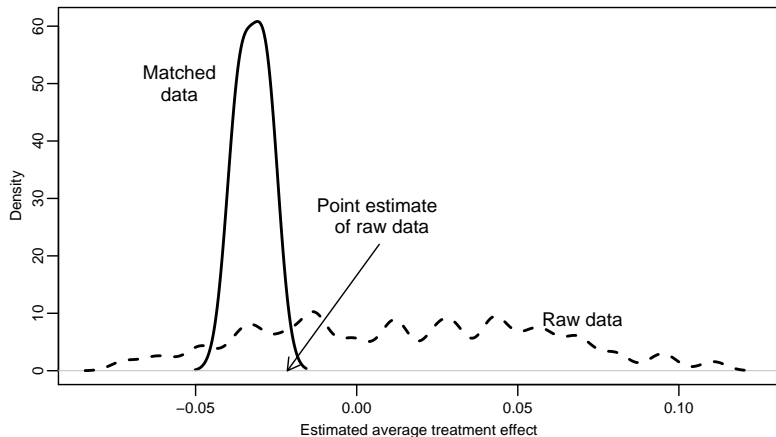


Figure: Estimated effects of being a highly visible female Republican candidate across 63 possible specifications with the Koch data.

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- Readers (and authors) need not worry that slightly different specifications alter the empirical conclusions.

<http://GKing.Harvard.edu>

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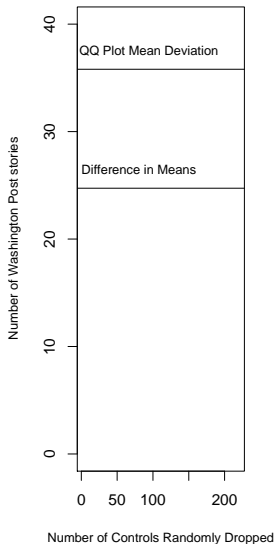
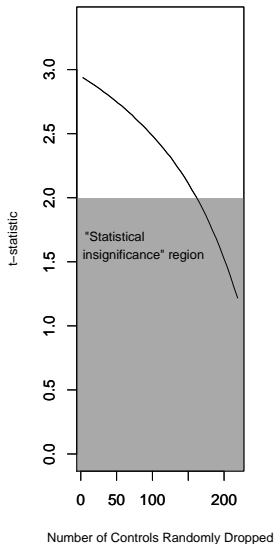
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 - I.e., it works when it works, and when it doesn't work, it doesn't work.

Hypothesis Tests for Balance Make No Sense



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- Could estimate multivariate density $P(X)$ and then compute hyper-volume near the counterfactual point: $\int_{x \in R} P(X) dX$.

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- Regression confidence intervals widen as \hat{y} 's are farther from the data. This does not include model uncertainty, but we could use it as an index of how far we are from the data.

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Omitted Variable Bias

