## Correcting Measurement Error Bias in Conjoint Survey Experiments ${ }^{1}$

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Stanford, Dartmouth, NYUAD, Harvard, Rochester

Society for Political Methodology, 7/10/2023
${ }^{1}$ Paper, software, slides, data: GaryKing.org/conjointE

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- How much? Lots!
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- Ignore it? Bias!
- Easy to fix? Estimate IRR \& a few lines of code
- Evidence: 13+ surveys, 9,472 respondents, 137,785 questions


## Conjoint Questions: Complicated Real World Trade Offs

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Please carefully review the two potential candidates running for election to the U.S. House of Representatives, detailed below.

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| Age |
| Favorability rating among the pub- |
| lic |
| Position on immigrants |
| Party affiliation |
| Position on abortion |
| Position on government deficit |
| Salient personal characteristics |
| Position on national security |
| Gender |
| Policy area of expertise |
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| Experience in public office |

\(\left.$$
\begin{array}{ll}\text { Candidate } 0 & \text { Candidate 1 } \\
\hline \text { Hispanic } & \text { Asian American } \\
52 & 60 \\
70 \% & 34 \% \\
\text { Favors giving citizenship or guest } \\
\text { worker status to undocumented } \\
\text { immigrants }\end{array}
$$ \quad \begin{array}{l}Opposes giving citizenship or guest <br>
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| :--- | :--- |
| Abortion is not a private matter <br> (pro-life) | Wants to reduce the deficit through <br> tax increase |
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| tax increase | Really cares about people like you |
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| Wants to cut military budget and | Wants to maintain strong defense <br> and increase U.S. influence |
| keep the U.S. out of war | Female |
| Female | Foreign policy |
| Education | Married (no child) |
| Single (divorced) | 4 years |
| 12 years |  |

If you had to choose between them, which of these candidates would you vote to be a member of the U.S. House of Representatives?

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- Same: measurement error corrections


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- Casual effect: Average Marginal Component Effect (AMCE)

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2. Calculate: $\hat{\tau}=\frac{1-\sqrt{1-2(1-\mathrm{IRR})}}{2}$

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- $\tau(a) \approx \tau$ : correction is easy


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Study

- Arias and Blair (2022)
$\rightarrow$ Bechtel and Scheve (2013)
$\rightarrow$ Blackman (2018)
$\rightarrow$ Hainmueller and Hopkins (2015)
$\rightarrow$ Hankinson (2018)
$\rightarrow$ Mummolo and Nall (2017)
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- Impressive literature, especially given crises in other fields


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- Estimate IRR separately for subgroup analysis


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## Consequences of Bias Correction in 8 Studies



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