Simplifying Matching Methods for Causal Inference

Gary King¹

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1. The most popular method (propensity score matching, used in 179,000 articles!) sounds magical:

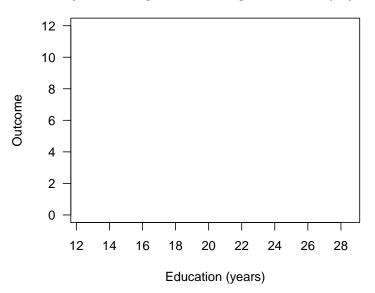
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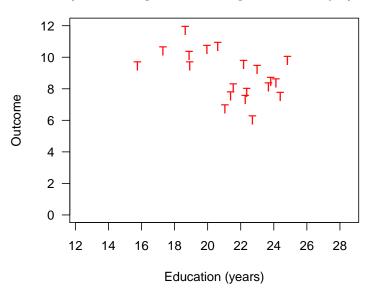
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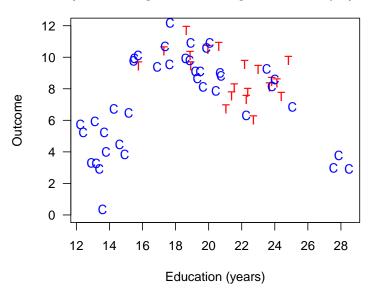
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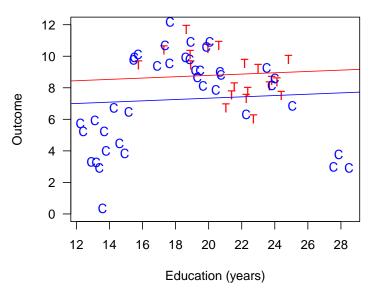
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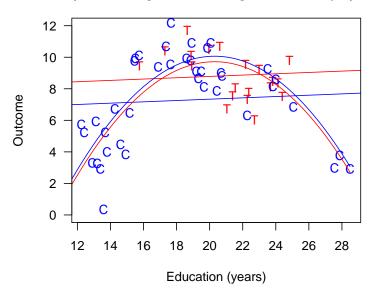
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 - "The Balance-Sample Size Frontier in Matching Methods for Causal Inference" (In press, AJPS; Gary King, Christopher Lucas and Richard Nielsen)

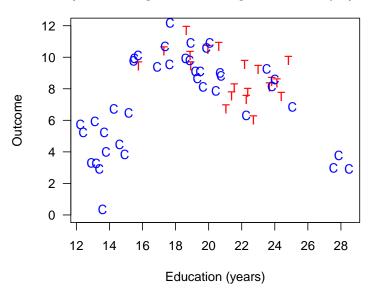


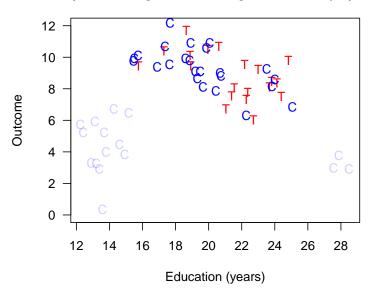


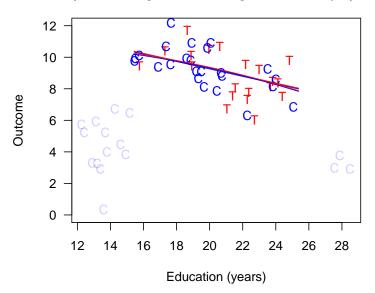












Without Matching:

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Imbalance

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Imbalance → Model Dependence

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Imbalance → Model Dependence → Researcher discretion → Bias

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- "Teaching psychology is mostly a waste of time" (Kahneman 2011)

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The Problems Matching Solves

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A central project of statistics: Automating away human discretion

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- Pruning nonmatches makes control vars matter less: reduces imbalance, model dependence, researcher discretion, & bias

Matching: Finding Hidden Randomized Experiments

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Complete Randomization

Complete Fully Randomization Blocked

Balance	Complete	Fully	
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Observed			
Unobserved			

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- Other methods: fully blocked
- Other matching methods dominate PSM (wait, it gets worse)

(Approximates Fully Blocked Experiment)

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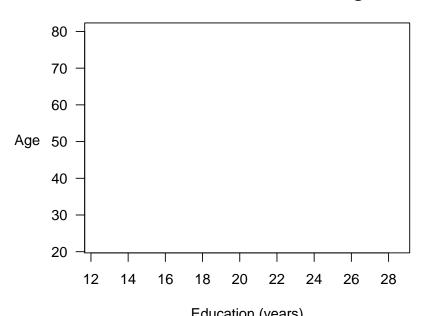
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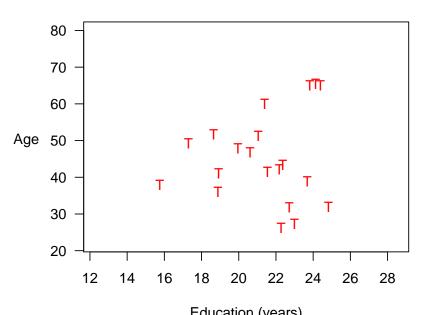
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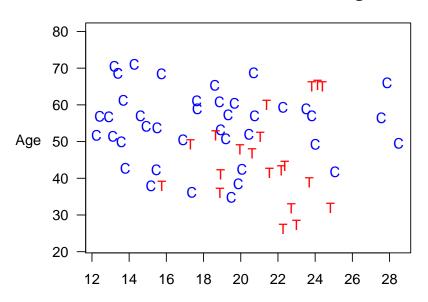
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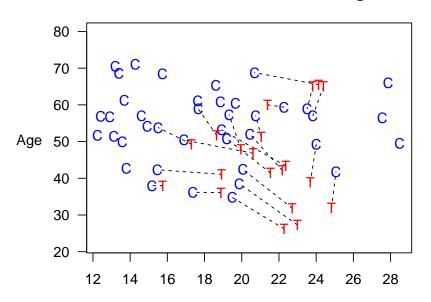
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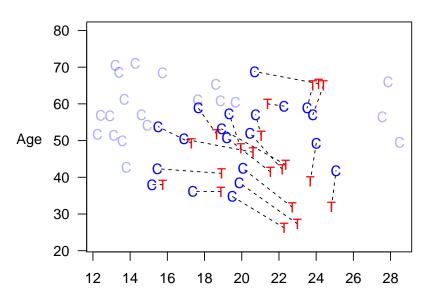
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 - (Many adjustments available to this basic method)
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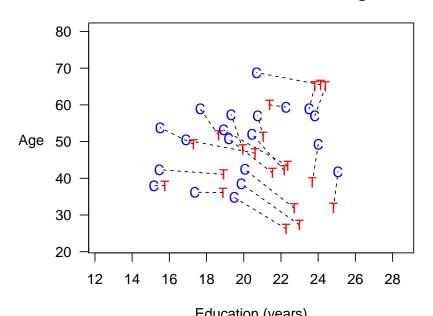


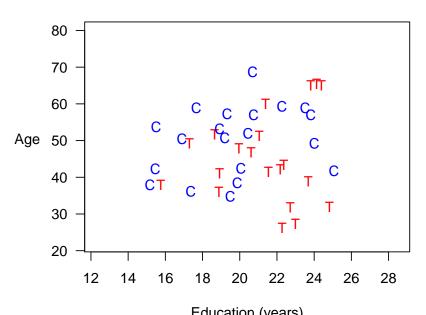






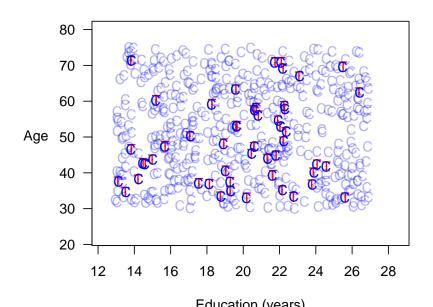




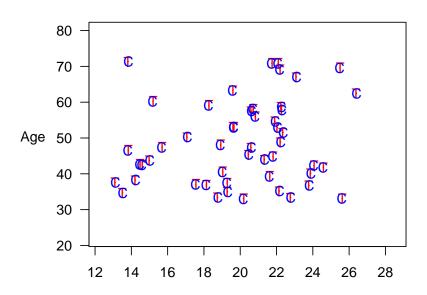


Best Case: Mahalanobis Distance Matching

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Method 2: Coarsened Exact Matching (Most powerful easy-to-use approach) (Approximates Fully Blocked Experiment)

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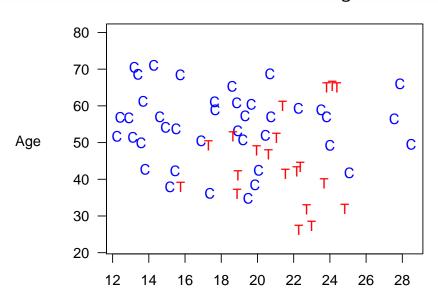
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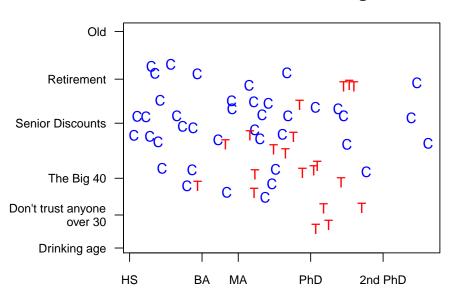
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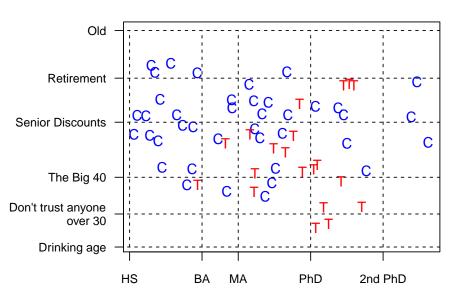
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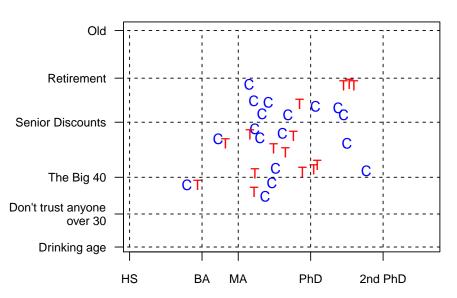
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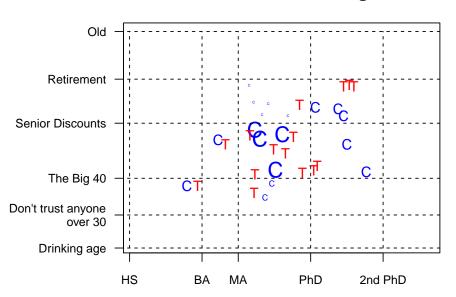






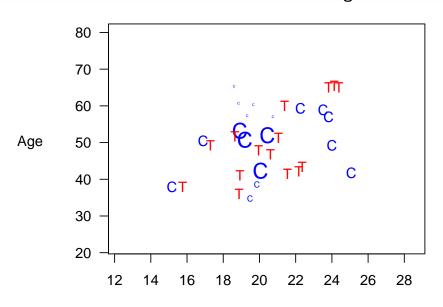
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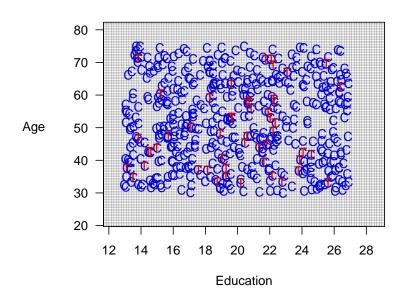
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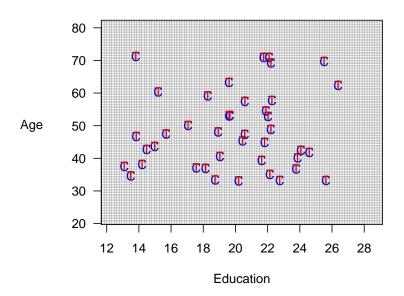


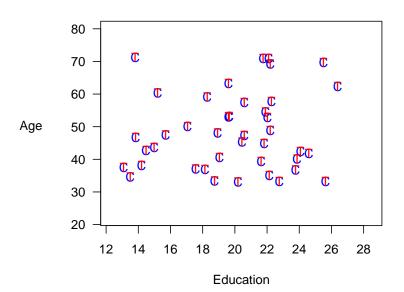
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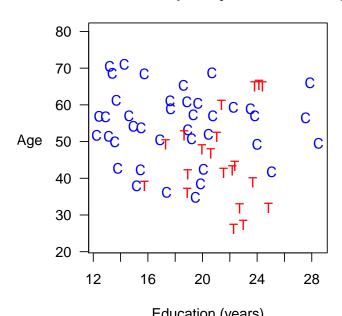
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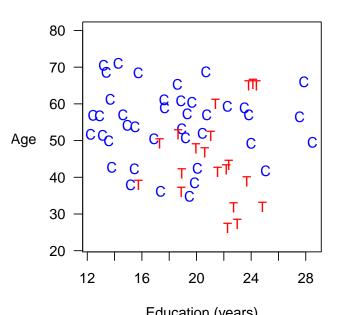
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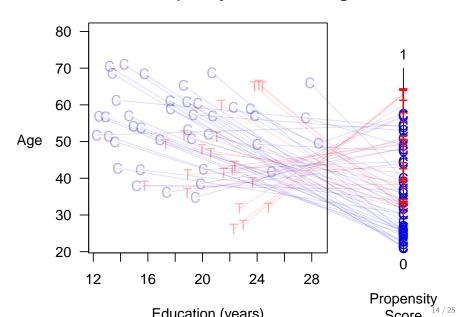
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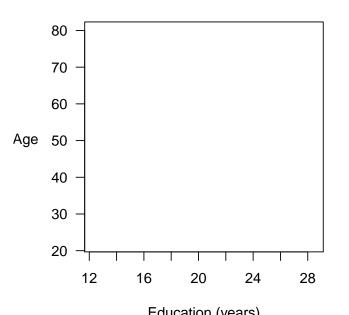
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 - · Control units: not reused; pruned if unused
 - Prune matches if Distance>caliper
 - (Many adjustments available to this basic method)
- 2. Estimation Difference in means or a model

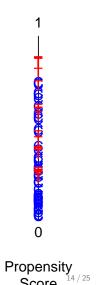


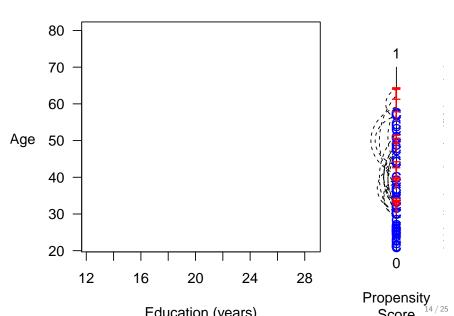


Propensity Score 14/25

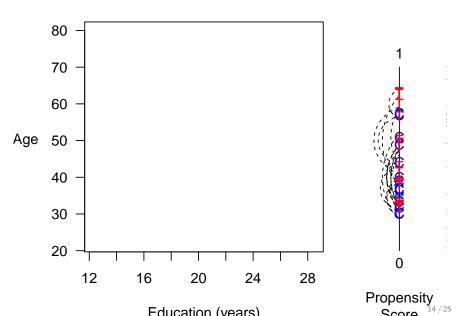




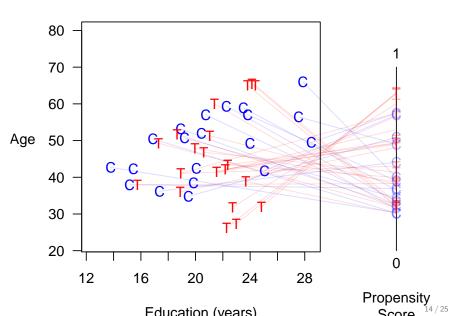


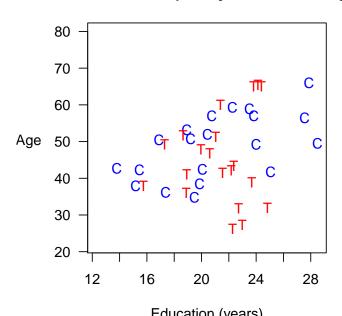


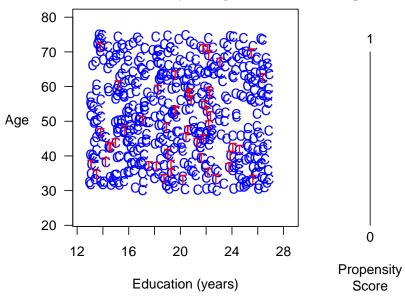
Education (years)

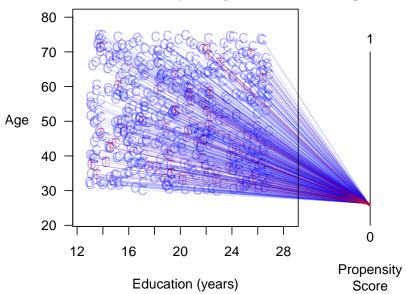


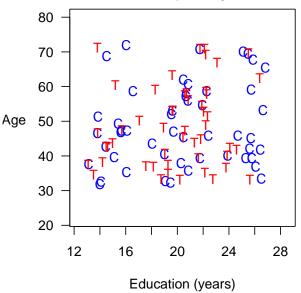
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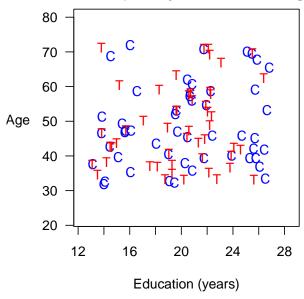








Best Case: Propensity Score Matching is Suboptimal



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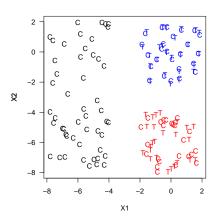
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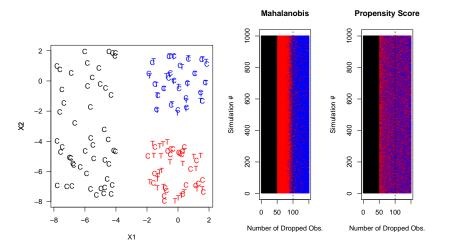
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- Doesn't PSM solve the curse of dimensionality problem?
 Nope. The PSM Paradox gets worse with more covariates

PSM is Blind Where Other Methods Can See

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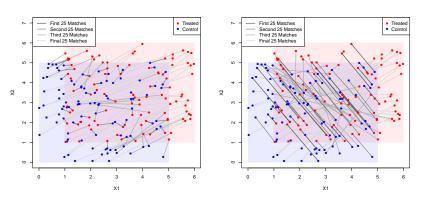
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What Does PSM Match?

MDM Matches

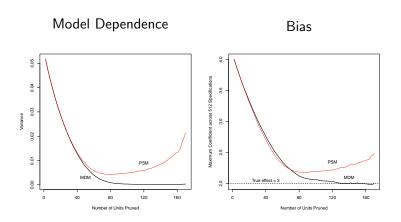
PSM Matches



Controls: $X_1, X_2 \sim \text{Uniform}(0,5)$

Treateds: $X_1, X_2 \sim \text{Uniform}(1,6)$

PSM Increases Model Dependence & Bias

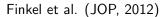


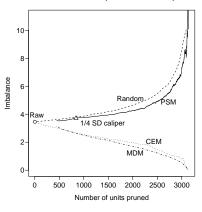
$$Y_i = 2T_i + X_{1i} + X_{2i} + \epsilon_i$$

$$\epsilon_i \sim N(0, 1)$$

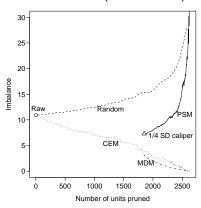
The Propensity Score Paradox in Real Data

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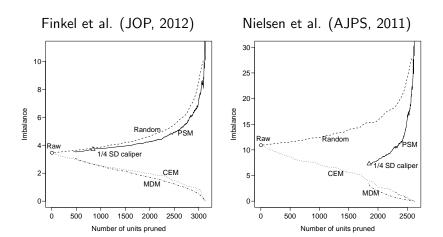




Nielsen et al. (AJPS, 2011)



The Propensity Score Paradox in Real Data



Similar pattern for > 20 other real data sets we checked

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- Choose an imbalance metric, then run.

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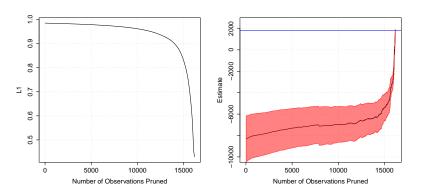
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Job Training Data: Frontier and Causal Estimates



- 185 Ts; pruning most 16,252 Cs won't increase variance much
- Huge bias-variance trade-off after pruning most Cs
- Estimates converge to experiment after removing bias
- No mysteries: basis of inference clearly revealed

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For more information, articles, & software

GaryKing.org