Matching Methods for Causal Inference

Gary King¹

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Harvard Health Policy and Insurance Research Seminar, 10/16/2017

¹GaryKing.org

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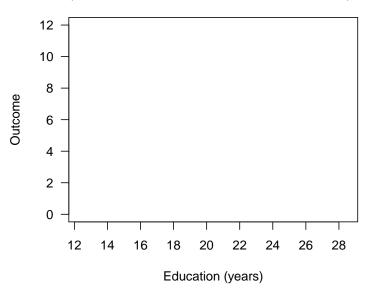
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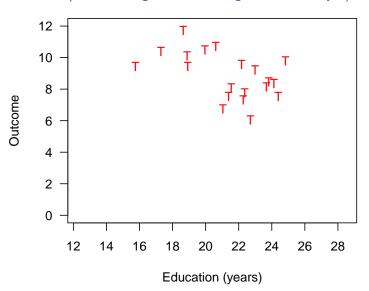
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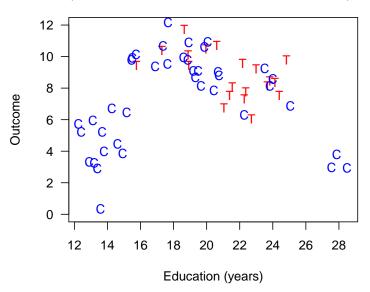
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 - "Causal Inference Without Balance Checking: Coarsened Exact Matching" (PA, 2011. Stefano M lacus, Gary King, and Giuseppe Porro)

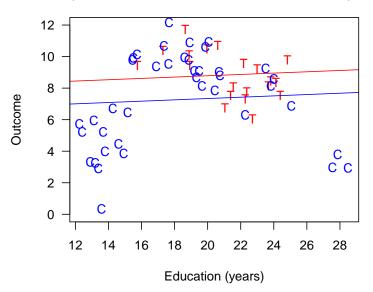
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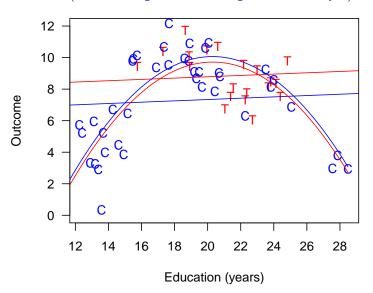
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 - "The Balance-Sample Size Frontier in Matching Methods for Causal Inference" (In press, AJPS; Gary King, Christopher Lucas and Richard Nielsen)

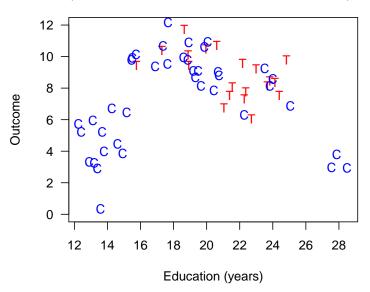


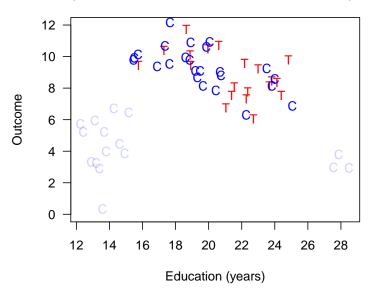


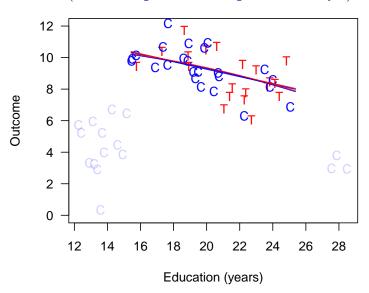












Without Matching:

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Imbalance

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Imbalance → Model Dependence

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- "Teaching psychology is mostly a waste of time" (Kahneman 2011)

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The Problems Matching Solves

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Model Dependence --> Researcher discretion --> Bias

A central project of statistics: Automating away human discretion

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- Pruning nonmatches makes control vars matter less: reduces imbalance, model dependence, researcher discretion, & bias

Complete Randomization

Complete Fully Randomization Blocked

Balance	Complete	Fully	
Covariates:	Randomization	Blocked	
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Unobserved			

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- Other methods: fully blocked
- Other matching methods dominate PSM

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- Other methods: fully blocked
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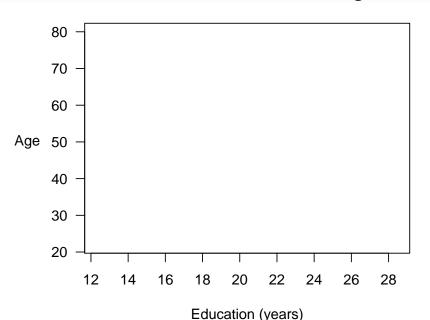
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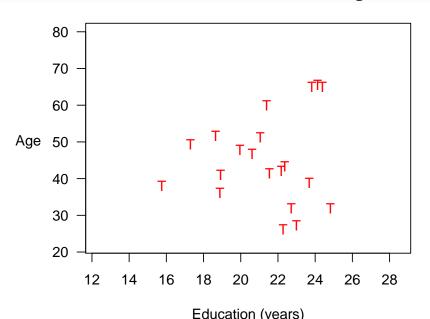
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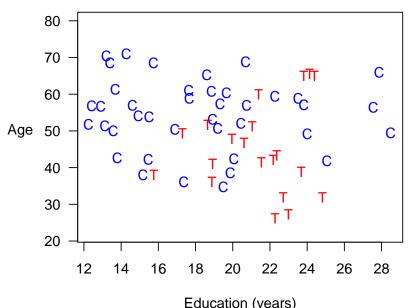
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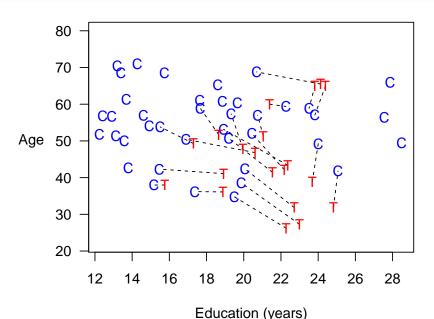
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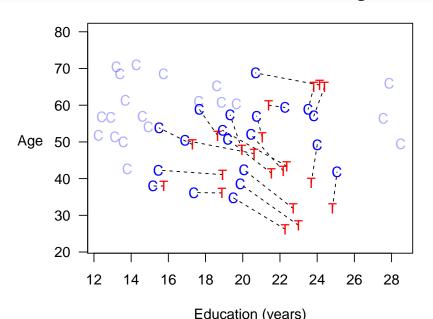
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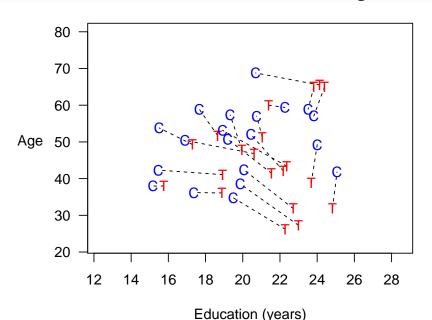


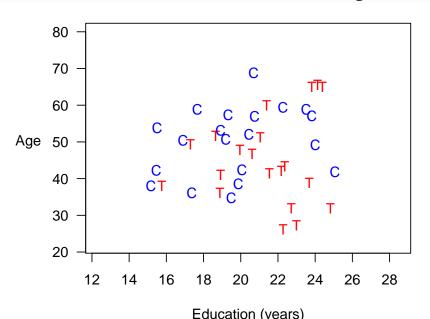






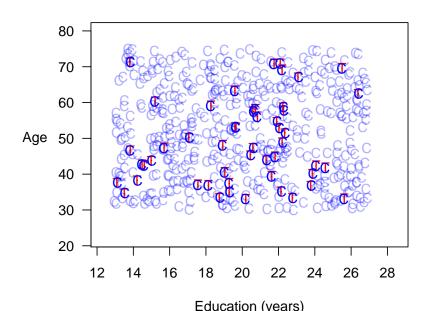




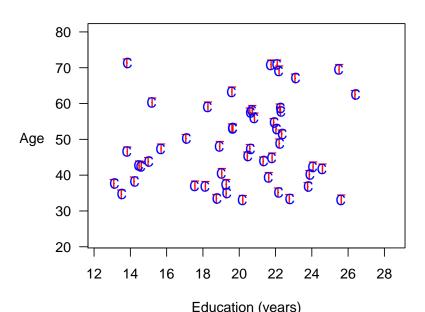


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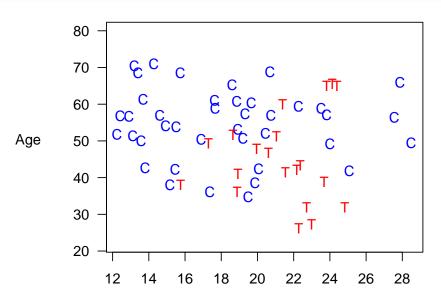
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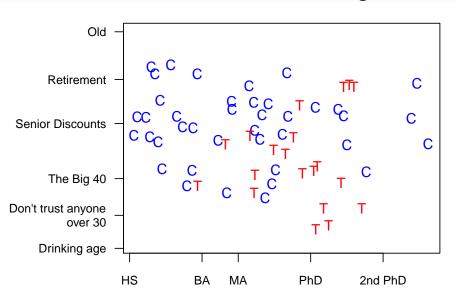
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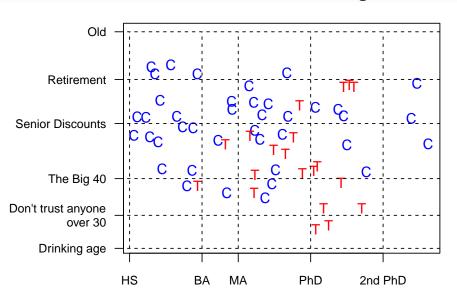
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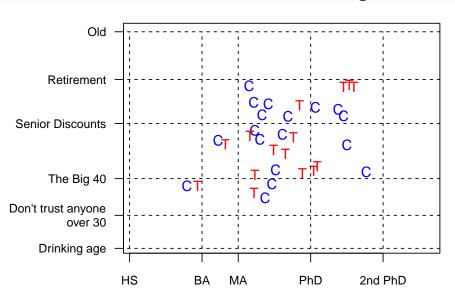
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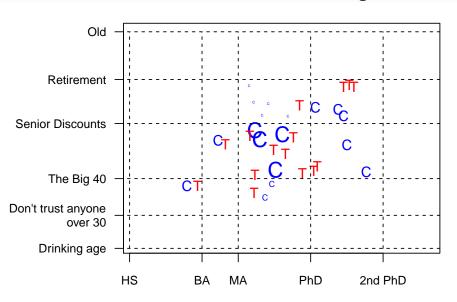
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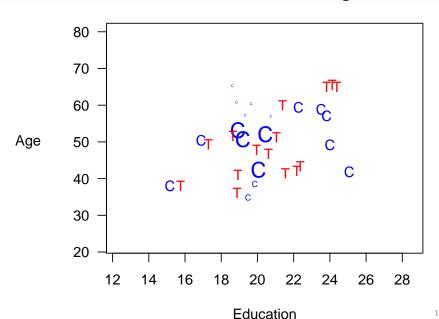


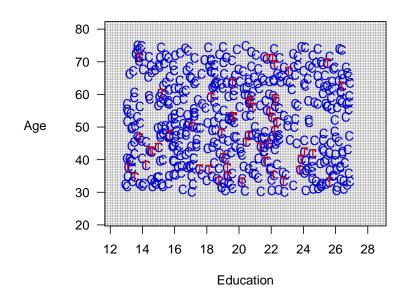


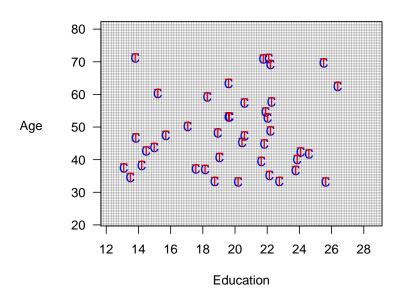
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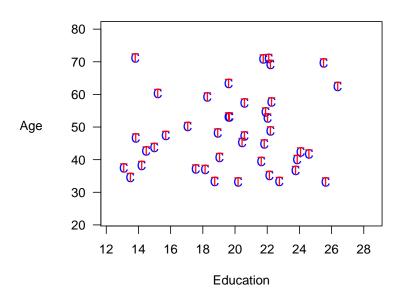


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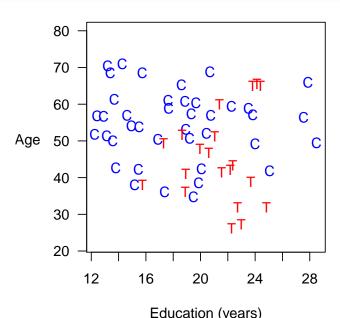
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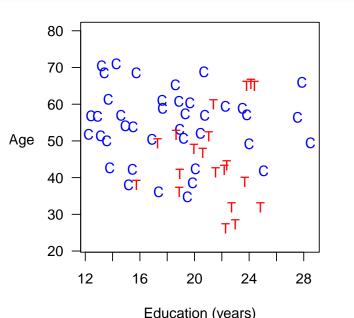
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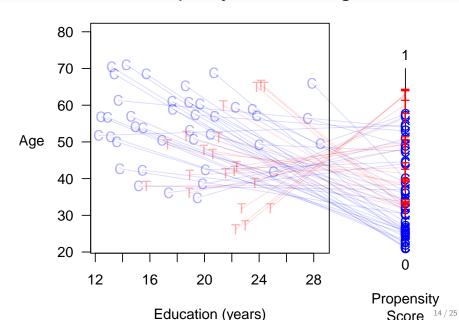
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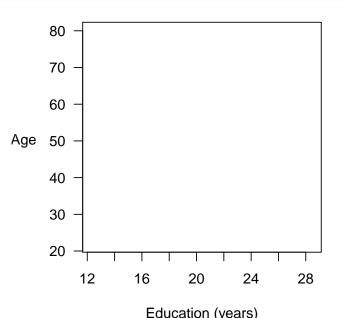


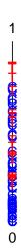


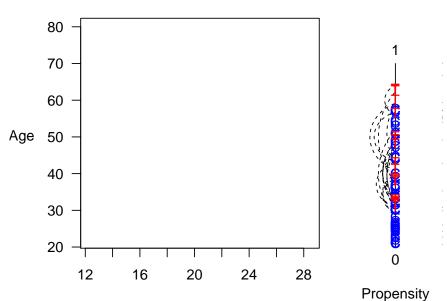
Propensity

Score



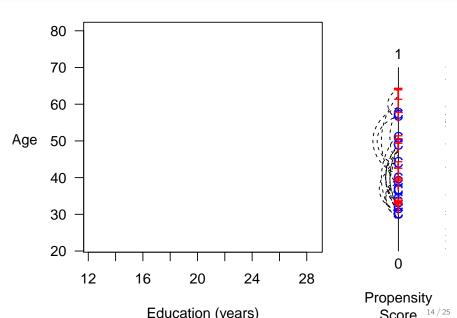




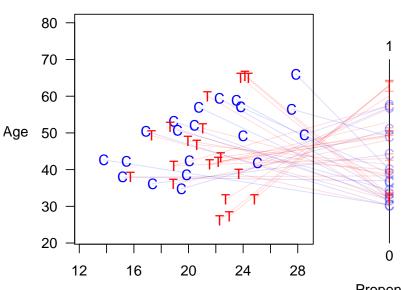


Education (years)

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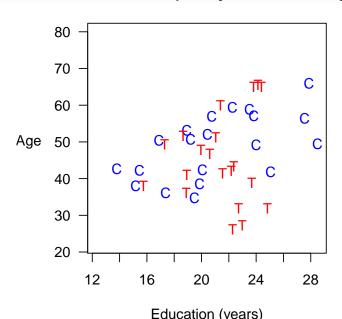


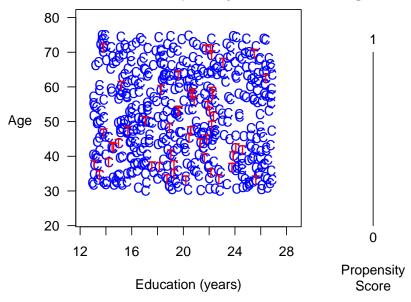
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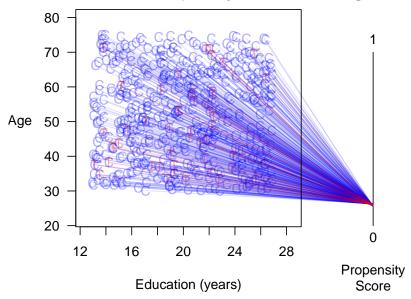


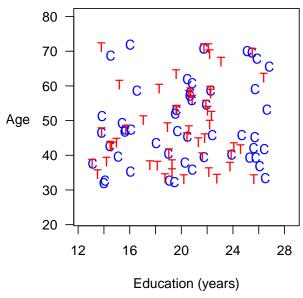
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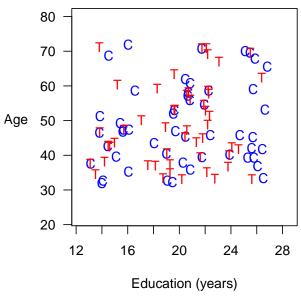








Best Case: Propensity Score Matching is Suboptimal



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 Nope.

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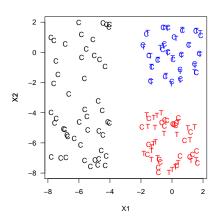
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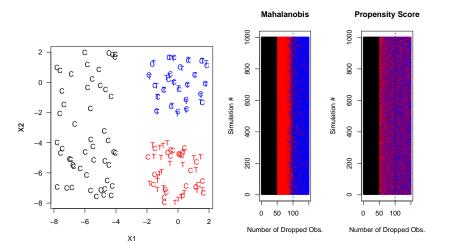
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 Nope. The PSM Paradox gets worse with more covariates

PSM is Blind Where Other Methods Can See

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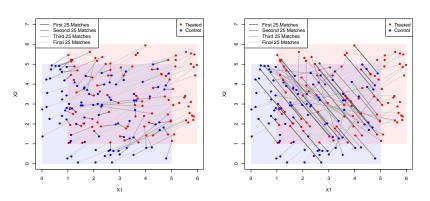
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What Does PSM Match?

MDM Matches

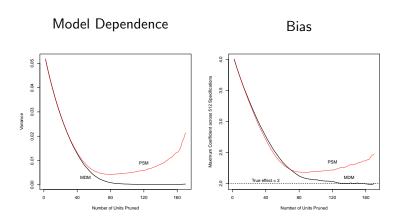
PSM Matches



Controls: $X_1, X_2 \sim \text{Uniform}(0,5)$

Treateds: $X_1, X_2 \sim \mathsf{Uniform}(1,6)$

PSM Increases Model Dependence & Bias

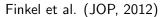


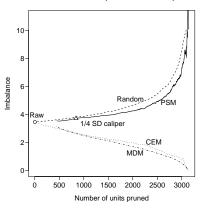
$$Y_i = 2T_i + X_{1i} + X_{2i} + \epsilon_i$$

$$\epsilon_i \sim N(0, 1)$$

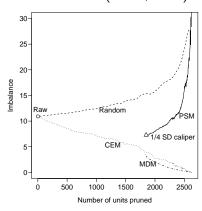
The Propensity Score Paradox in Real Data

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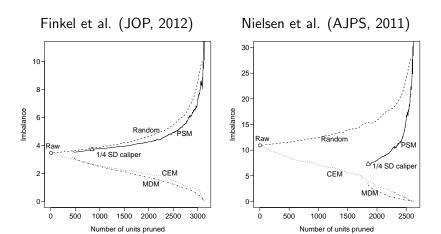




Nielsen et al. (AJPS, 2011)



The Propensity Score Paradox in Real Data



Similar pattern for > 20 other real data sets we checked

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- Choose an imbalance metric, then run.

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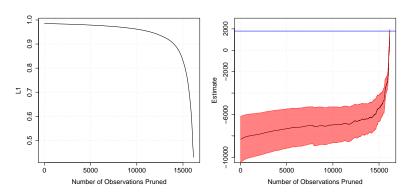
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Job Training Data: Frontier and Causal Estimates



- 185 Ts; pruning most 16,252 Cs won't increase variance much
- Huge bias-variance trade-off after pruning most Cs
- Estimates converge to experiment after removing bias
- No mysteries: basis of inference clearly revealed

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For more information, articles, & software

GaryKing.org