# Matching Methods for Causal Inference & 21 Other Topics

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1. The most popular method (propensity score matching, used in 76,900 articles!) sounds magical:

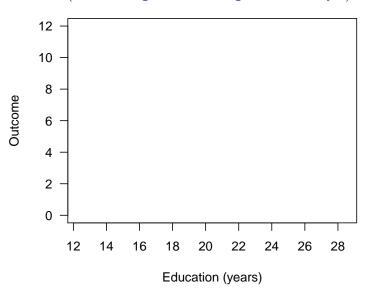
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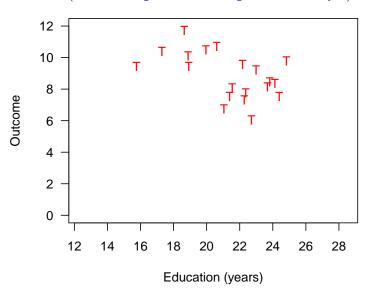
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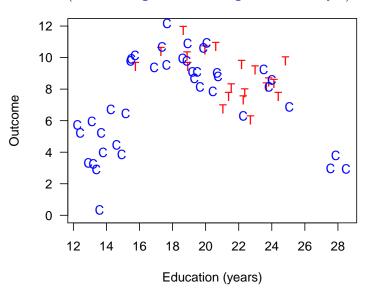
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  - "Causal Inference Without Balance Checking: Coarsened Exact Matching" (PA, 2011. Stefano M lacus, Gary King, and Giuseppe Porro)

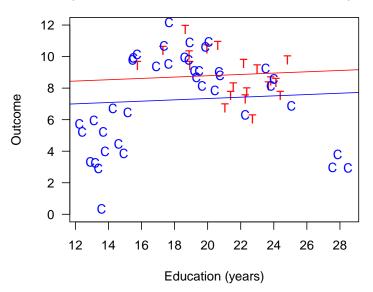
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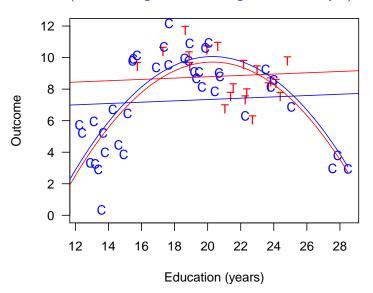
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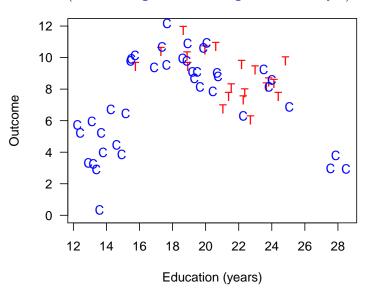


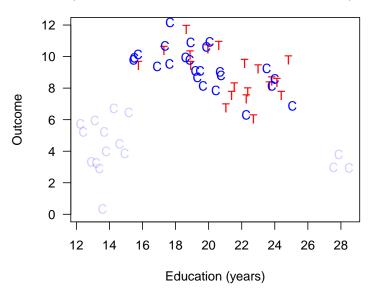


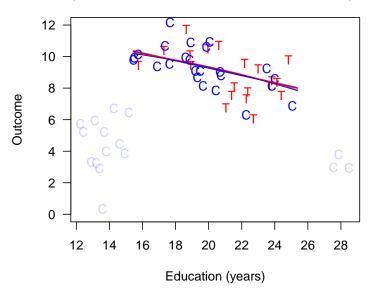












Without Matching:

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**Imbalance** 

Without Matching:

Imbalance → Model Dependence

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- "Teaching psychology is mostly a waste of time" (Kahneman 2011)

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## The Problems Matching Solves

Without Matching:

Model Dependence --> Researcher discretion --> Bias

A central project of statistics: Automating away human discretion

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- Pruning nonmatches makes control vars matter less: reduces imbalance, model dependence, researcher discretion, & bias

Complete Randomization

Complete Fully Randomization Blocked

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Unobserved		

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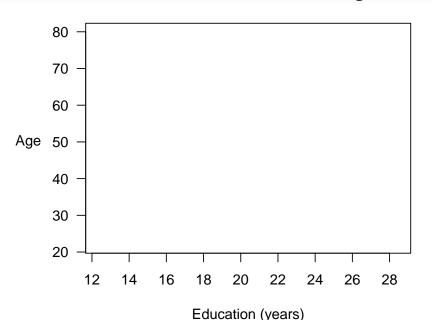
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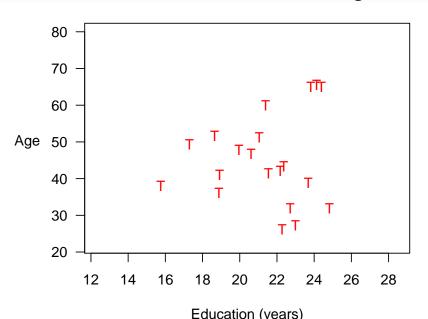
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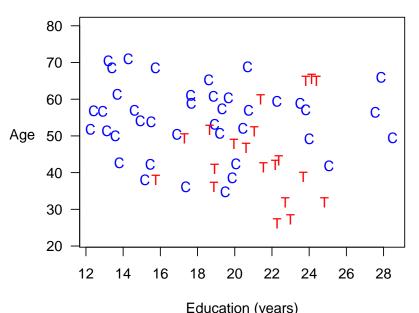
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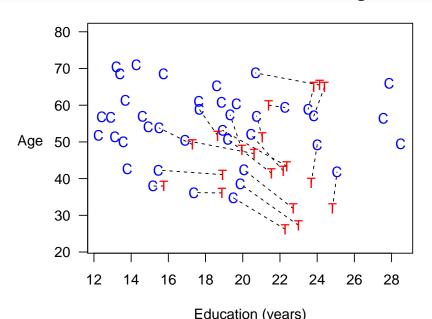
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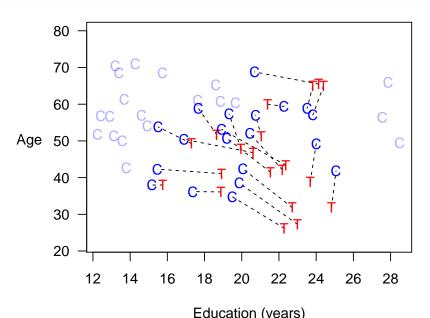
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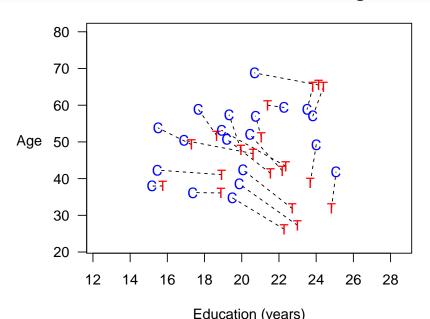


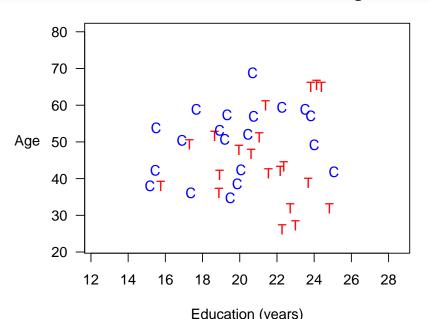






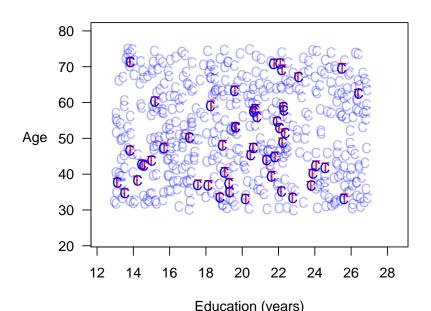




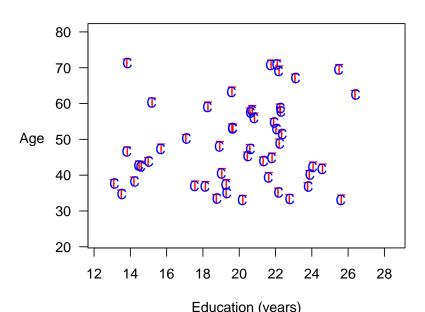


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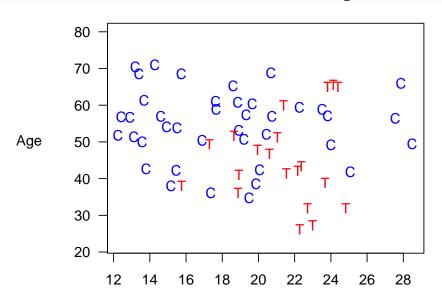
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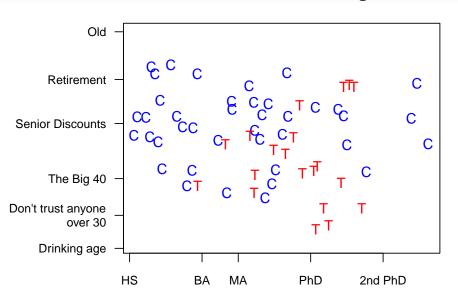
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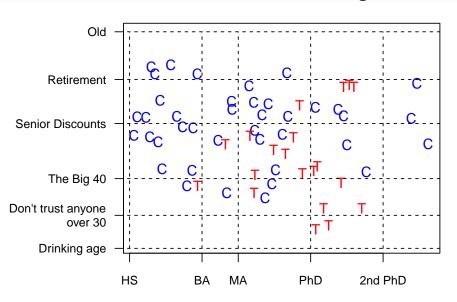
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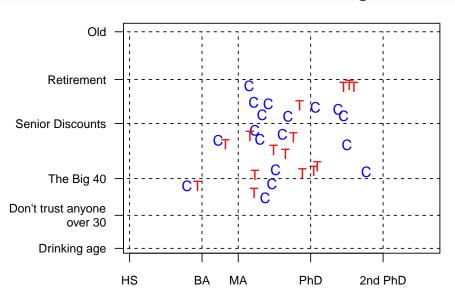
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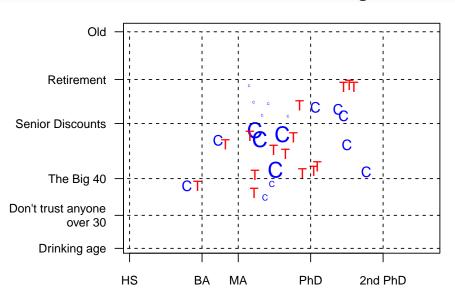




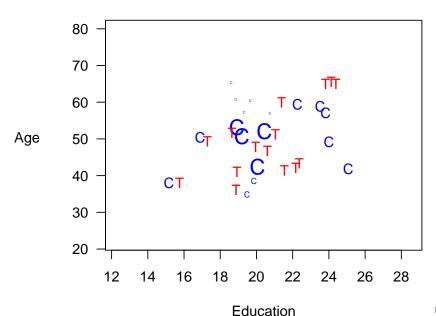


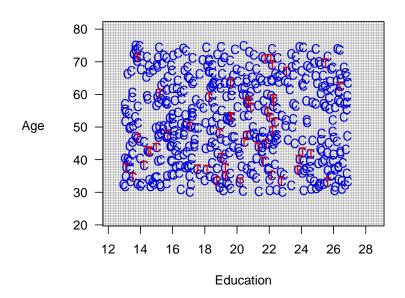


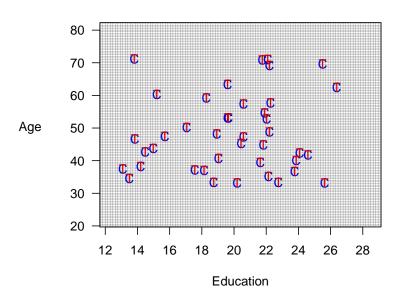
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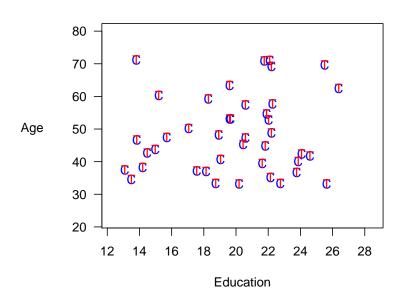


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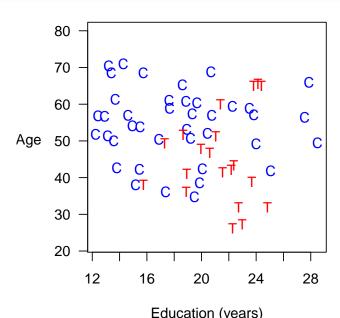
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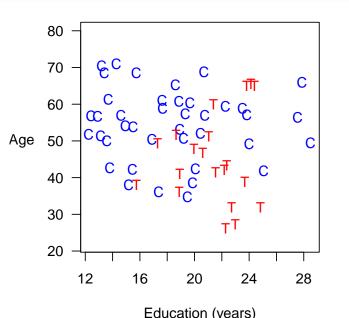
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  - Prune matches if Distance>caliper
- 2. Estimation Difference in means or a model

(Approximates Completely Randomized Experiment)

- 1. Preprocess (Matching)
  - Reduce k elements of X to scalar  $\pi_i \equiv \Pr(T_i = 1 | X) = \frac{1}{1 + e^{-X_i \beta}}$
  - Distance $(X_c, X_t) = |\pi_c \pi_t|$
  - Match each treated unit to the nearest control unit
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  - (Many adjustments available to this basic method)
- 2. Estimation Difference in means or a model

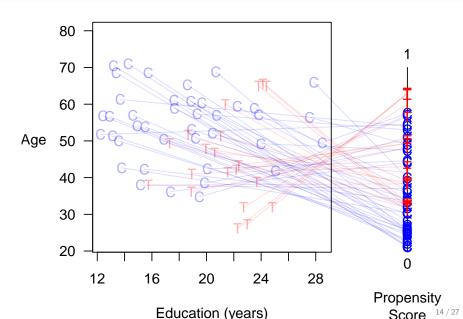


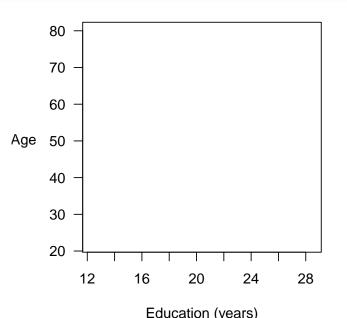




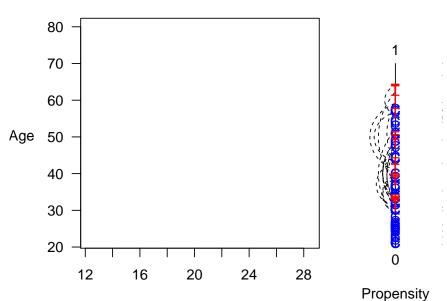
Propensity

Score



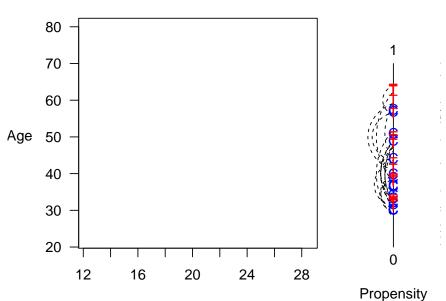






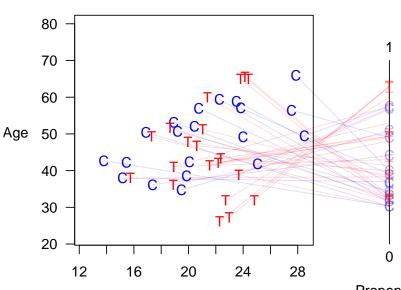
Education (years)

Score 14/27



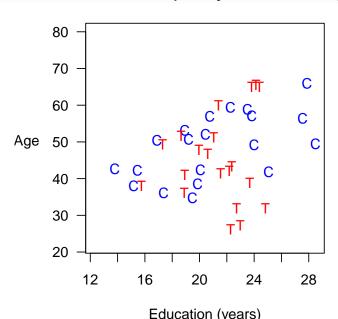
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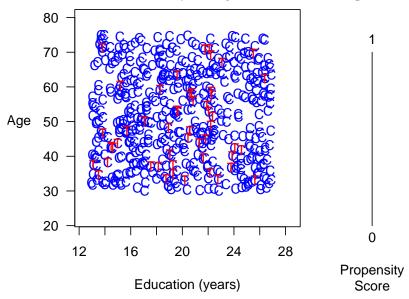
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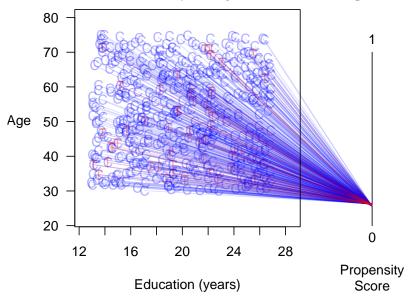


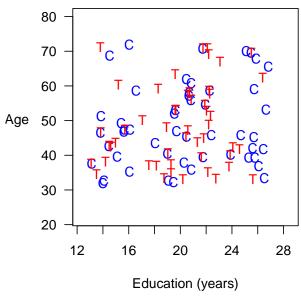
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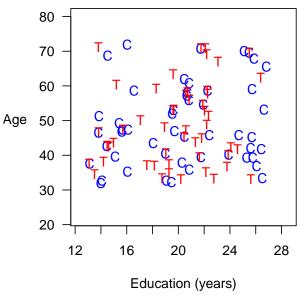








# Best Case: Propensity Score Matching is Suboptimal



Deleting data only helps if you're careful!

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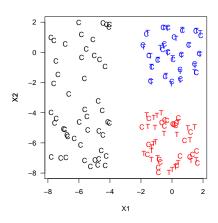
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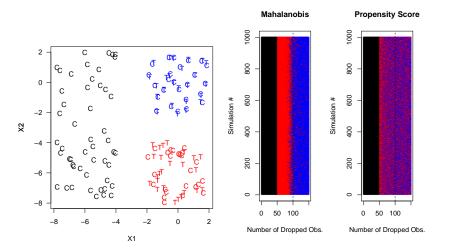
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### PSM is Blind Where Other Methods Can See

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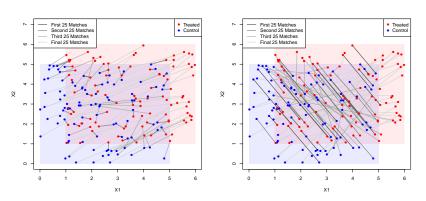
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#### What Does PSM Match?

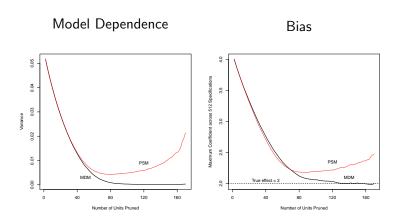


#### PSM Matches



Controls:  $X_1, X_2 \sim \text{Uniform}(0,5)$ Treateds:  $X_1, X_2 \sim \text{Uniform}(1,6)$ 

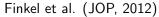
## PSM Increases Model Dependence & Bias

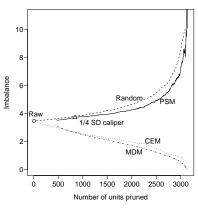


$$Y_i = 2T_i + X_{1i} + X_{2i} + \epsilon_i$$
  
$$\epsilon_i \sim N(0, 1)$$

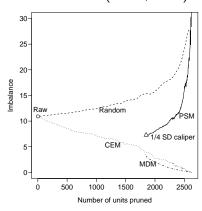
## The Propensity Score Paradox in Real Data

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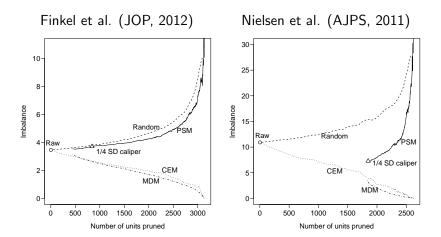




#### Nielsen et al. (AJPS, 2011)



### The Propensity Score Paradox in Real Data



Similar pattern for > 20 other real data sets we checked

# The Matching Frontier

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- Choose an imbalance metric, then run.

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  - e.g., N > 300 requires more imbalance evaluations than elementary particles in the universe

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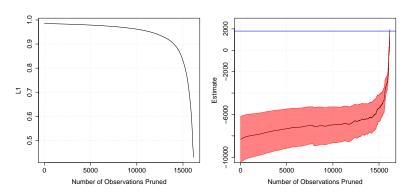
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# Job Training Data: Frontier and Causal Estimates



- 185 Ts; pruning most 16,252 Cs won't increase variance much
- Huge bias-variance trade-off after pruning most Cs
- Estimates converge to experiment after removing bias
- No mysteries: basis of inference clearly revealed

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