# Comparative Effectiveness of Matching Methods for Causal Inference

#### Gary King Institute for Quantitative Social Science Harvard University

joint work with

Richard Nielsen (Harvard), Carter Coberley, James Pope, Aaron Wells (Healthways)

Talk at Quantitative Issues in Cancer Research Working Seminar, Biostatistics, HSPH, 10/18/10

#### • Problem: Model dependence (review)

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- Solution: Matching to preprocess data (review)

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- Solution: The Space Graph helps us compare
- Problem: The most commonly used method can increase imbalance!
- Solution: Other methods do not share this problem
- $\bullet \, \rightsquigarrow$  Lots of insights revealed in the process

### Model Dependence Demonstration

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- Data analysis: Logit model
- The question: How model dependent are the results?

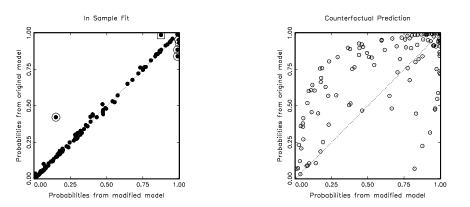
# Two Logit Models, Apparently Similar Results

	Original "Interactive" Model			Modified Model		
Variables	Coeff	SE	P-val	Coeff	SE	P-val
Wartype	-1.742	.609	.004	-1.666	.606	.006
Logdead	445	.126	.000	437	.125	.000
Wardur	.006	.006	.258	.006	.006	.342
Factnum	-1.259	.703	.073	-1.045	.899	.245
Factnum2	.062	.065	.346	.032	.104	.756
Trnsfcap	.004	.002	.010	.004	.002	.017
Develop	.001	.000	.065	.001	.000	.068
Exp	-6.016	3.071	.050	-6.215	3.065	.043
Decade	299	.169	.077	-0.284	.169	.093
Treaty	2.124	.821	.010	2.126	.802	.008
UNOP4	3.135	1.091	.004	.262	1.392	.851
Wardur*UNOP4	—	—	—	.037	.011	.001
Constant	8.609	2.157	0.000	7.978	2.350	.000
Ν	122			122		
Log-likelihood	-45.649			-44.902		
Pseudo R <sup>2</sup>		.423			.433	

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### Doyle and Sambanis: Model Dependence



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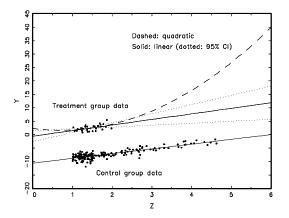
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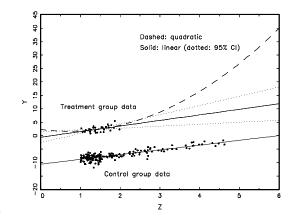
### Model Dependence: A Simpler Example

Gary King (Harvard, IQSS)

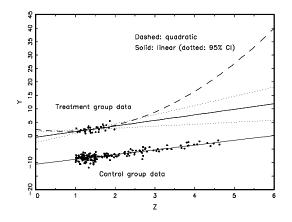
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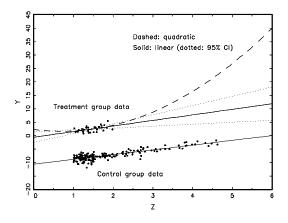


What to do?



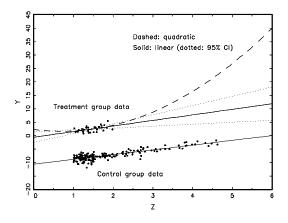
What to do?

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- Preprocess I: Eliminate extrapolation region
- Preprocess II: Match (prune bad matches) within interpolation region
- Model remaining imbalance

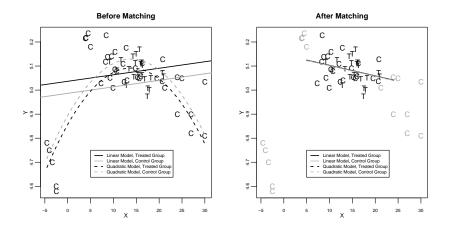
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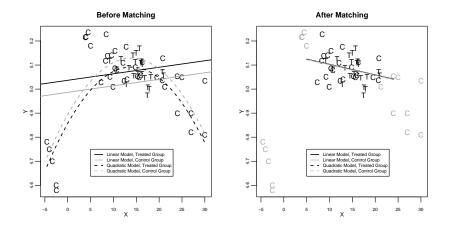
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Matching reduces model dependence, bias, and variance

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• or Feasible Average Treatment effect on the Treated: FSATT

# Method 1: Mahalanobis Distance Matching

Gary King (Harvard, IQSS)

#### Estimation Difference in means or a model

• Distance
$$(X_i, X_j) = \sqrt{(X_i - X_j)' S^{-1}(X_i - X_j)}$$

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- Stimation Difference in means or a model

# Method 2: Propensity Score Matching

Gary King (Harvard, IQSS)

#### **2** Estimation Difference in means or a model

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• Reduce k elements of X to scalar  $\pi_i \equiv \Pr(T_i = 1|X) = \frac{1}{1+e^{-X_i\beta}}$ 

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# Method 3: Coarsened Exact Matching

Gary King (Harvard, IQSS)

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  - Can apply other matching methods within CEM strata (inherit CEM's properties)

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- Measuring Imbalance
  - Classic measure: Difference of means (for each variable)
  - Better measure (difference of multivariate histograms):

$$\mathcal{L}_1(f,g;H) = rac{1}{2} \sum_{\ell_1 \cdots \ell_k \in H(\mathbf{X})} |f_{\ell_1 \cdots \ell_k} - g_{\ell_1 \cdots \ell_k}|$$

# Comparing Matching Methods

Gary King (Harvard, IQSS)

• MDM & PSM: Choose matched n, match, check imbalance

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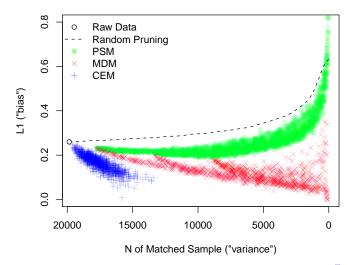
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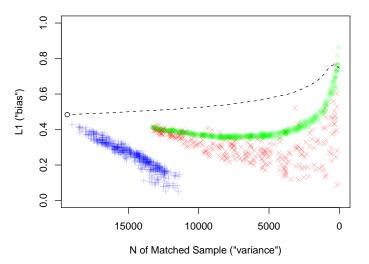
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- Choose matched solution & matching method becomes irrelevant
- Our idea: Compute lots of matching solutions, identify the frontier of lowest imbalance for each given *n*, and choose a matching solution

#### **Healthways Data**

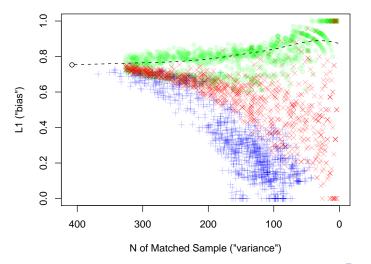


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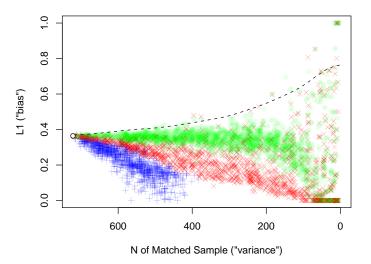
**Called/Not Called Data** 



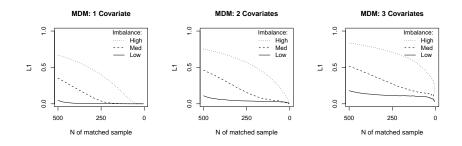




Lalonde Data Subset



#### A Space Graph: Simulated Data — Mahalanobis



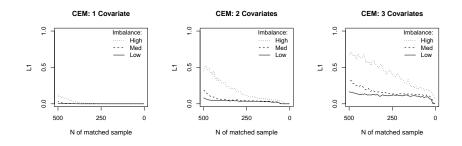
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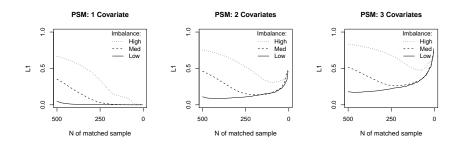
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### A Space Graph: Simulated Data — CEM



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### A Space Graph: Simulated Data — Propensity Score



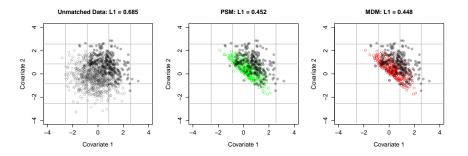
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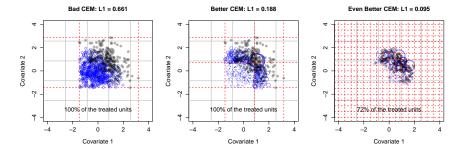
# Data where PSM Works Reasonably Well — PSM & MDM



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### Data where PSM Works Reasonably Well — CEM



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 (Unnormalized)

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• Gives a better pscore than PSM

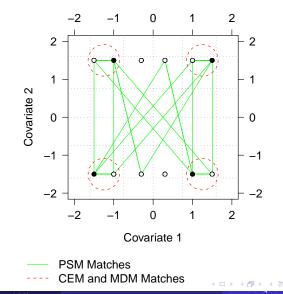
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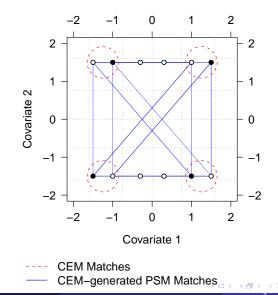
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- Gives a better pscore than PSM
- Doesn't match based on crippled information

# PSM Approximates Random Matching in Balanced Data



# Destroying CEM with PSM's Two Step Approach



Gary King (Harvard, IQSS)

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- You can easily check with the Space Graph

For papers, software (for R and Stata), tutorials, etc.

# http://GKing.Harvard.edu/cem

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