Statistically Valid Inferences from Privacy Protected Data¹

Gary King²

Institute for Quantitative Social Science Harvard University

Interagency Arctic Research Policy Committee, 11/19/2020

 $^{^1 \}hbox{Joint with Georgina Evans, Margaret Schwenzfeier, Abhradeep Thakurta.}$

²GaryKing.org/dp

Solving Political Problems Technologically

Differential Privacy & Inferential Validity

A General Purpose, Statistically Valid DP Algorithm

The Algorithm in Practice

Solving a Political Problem Technologically (via "constitutional design")

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- New Problem: Sharing data without it leaving Facebook

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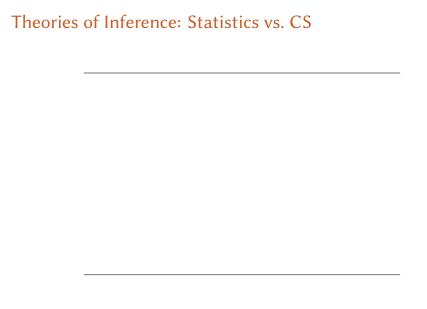
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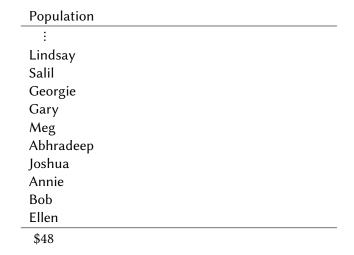
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Quantity of Interest

Mean

income:

Population	Sample	
:	X	
Lindsay	✓	
Salil	✓	
Georgie	✓	
Gary	✓	
Meg	✓	
Abhradeep	✓	
Joshua	✓	
Annie	✓	
Bob	✓	
Ellen	✓	
\$48		

Mean income: \$48

Quantity of Interest

Population	Sample	\$	
:	X	?	
Lindsay	✓	122	
Salil	✓	76	
Georgie	✓	145	
Gary	✓	96	
Meg	✓	86	
Abhradeep	✓	127	
Joshua	✓	72	
Annie	✓	132	
Bob	✓	95	
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\$48 Classic		- \$108	
Infere	nce		
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Georgie	✓	145	Noise	
Gary	✓	96		
Meg	✓	86	& •	
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Ellen	✓	134		201
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$$M(\text{mean}, D) = \frac{1}{n} \sum_{i=1}^{n} c(y_i, \Lambda) + N\left(0, \frac{8\Lambda}{n\epsilon}\right)$$
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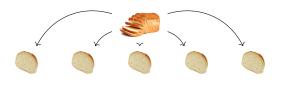
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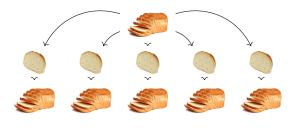


Private data



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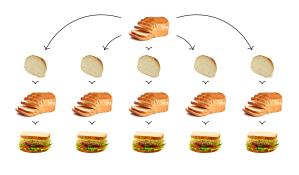
Partition



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Bag of little bootstraps

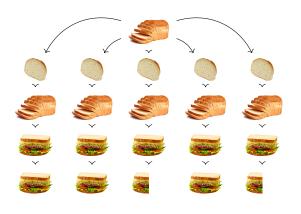


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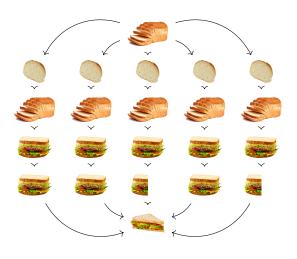
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Censor



Private data

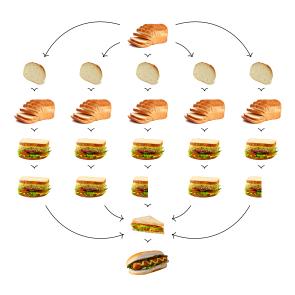
Partition

Bag of little bootstraps

Estimator

Censor

Average



Private data

Partition

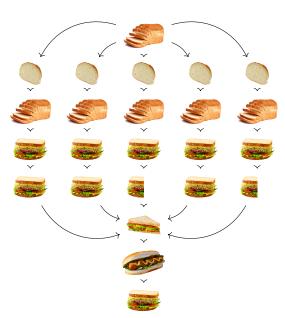
Bag of little bootstraps

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Censor

Average

Noise



Private data

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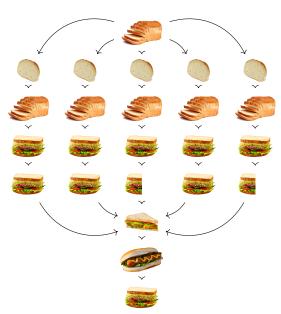
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Bias Correction



Private data

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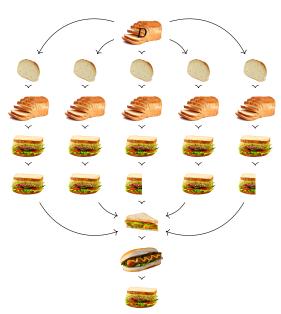
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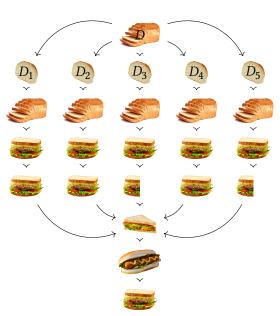
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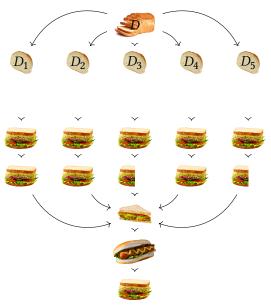
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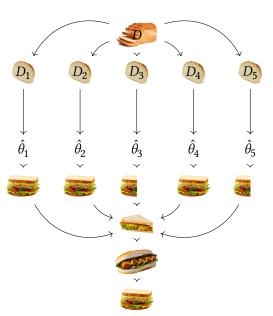
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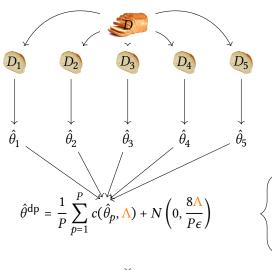
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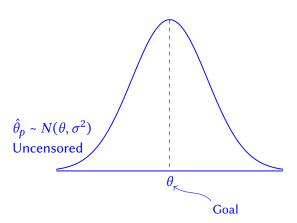
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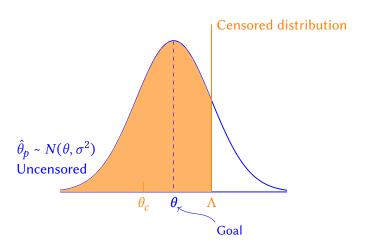
Bias Correction (& variance estimation)

Bias Correction of: $\hat{\theta}^{dp} = \frac{1}{P} \sum_{p=1}^{P} c(\hat{\theta}_p, \Lambda) + N(0, \frac{8\Lambda}{P\epsilon})$ (Λ, P, ϵ known)

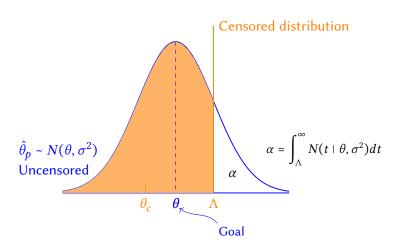
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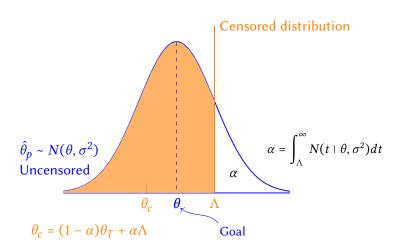
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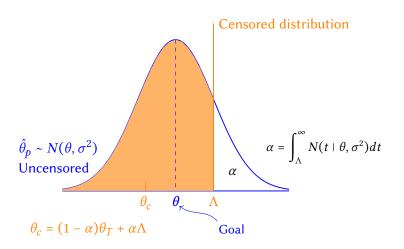
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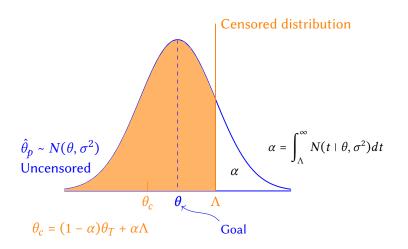


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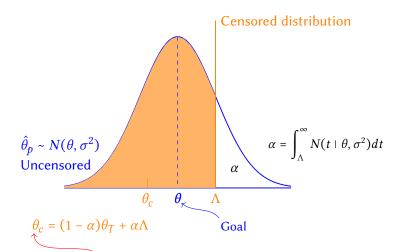
Equations: 2

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Unknowns: θ , σ^2 , α , θ_c

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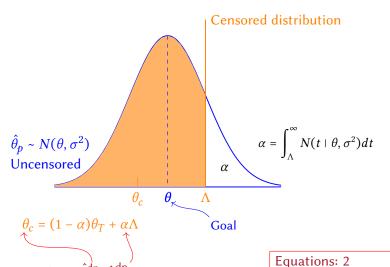


Disclose: $\hat{\theta}^{dp}$

Equations: 2

Unknowns: θ , σ^2 , α , κ

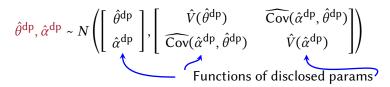
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Simulate estimates via standard (Clarify) procedures:

$$\hat{\theta}^{\mathsf{dp}}, \hat{\alpha}^{\mathsf{dp}} \sim N \left(\left[\begin{array}{c} \hat{\theta}^{\mathsf{dp}} \\ \hat{\alpha}^{\mathsf{dp}} \end{array} \right], \left[\begin{array}{cc} \hat{V}(\hat{\theta}^{\mathsf{dp}}) & \widehat{\mathsf{Cov}}(\hat{\alpha}^{\mathsf{dp}}, \hat{\theta}^{\mathsf{dp}}) \\ \widehat{\mathsf{Cov}}(\hat{\alpha}^{\mathsf{dp}}, \hat{\theta}^{\mathsf{dp}}) & \hat{V}(\hat{\alpha}^{\mathsf{dp}}) \end{array} \right] \right)$$

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Functions of disclosed params

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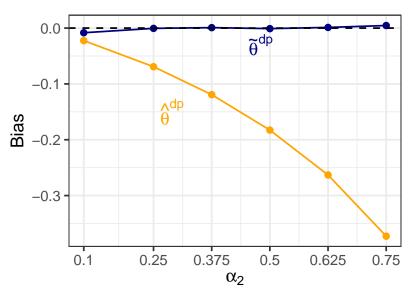
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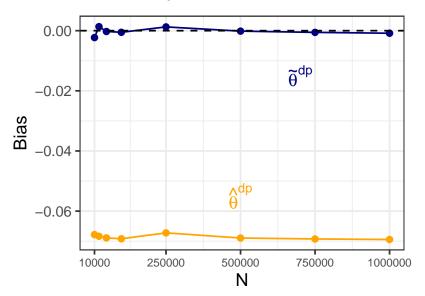
- Standard error: Standard deviation of $\tilde{\theta}^{dp}$ over simulations
- Bias correction: reduces bias and variance

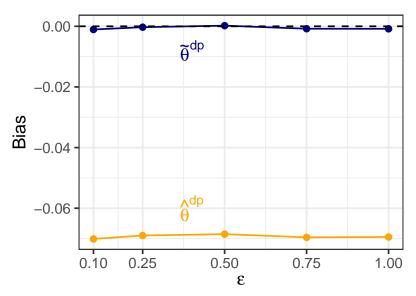
Solving Political Problems Technologically

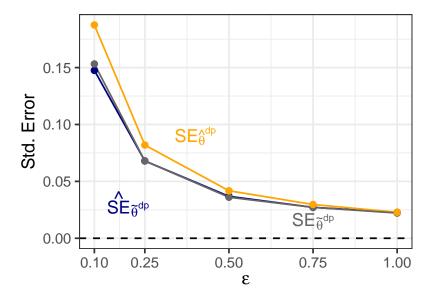
Differential Privacy & Inferential Validity

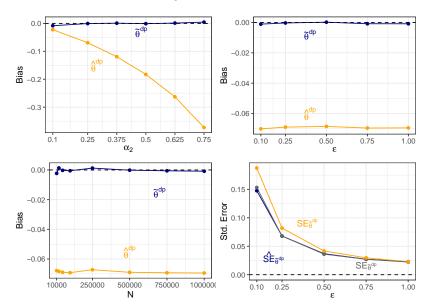
A General Purpose, Statistically Valid DP Algorithm











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 - Facebook, Microsoft+Harvard/IQSS, OpenDP

For more information



Georgina-Evans.com



GaryKing.org



MegSchwenzfeier.com



bit.ly/AbhradeepThakurta

Paper, software, slides, video: GaryKing.org/dp

Appendix

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